

Estimation

Learn by heart

- → An estimate is an approximate answer; not the exact answer.
- → To estimate: try rounding numbers to 1 significant figure before calculating.
- → Dividing by 0.5 is the same as multiplying by 2.
- Remember dividing by a number is the same as multiplying by its reciprocal.
- → ≈ means "is approximately equal to" = means "is exactly equal to".

Examples

Estimate
$$38.7 \times 5.8 \approx \frac{40 \times 6}{10} = \frac{240}{10} = 24$$

Estimate
$$\frac{19.2 + \sqrt{81}}{0.48} \approx \frac{20 + \sqrt{81}}{0.5}$$

$$= \frac{20 + 9}{0.5}$$

$$= \frac{29}{0.5}$$

$$= 58$$
(Dividing by 0.5 is the same as multiplying by 2)



Estimation

$$\rightarrow$$
 Estimate $\sqrt{42}$

Solution
$$\sqrt{36} = 6 , \sqrt{49} = 7$$

so
$$\sqrt{42} \approx 6.5$$

Ellen drives an average of 43.6 miles per week.
 (a) Work out an estimate for the number of miles Ellen drives in a year.

Solution

There are 52 weeks in a year

Ellen drives approximately 2000 miles in a year.

(b) Is your answer to part (a) an underestimate or an overestimate?

Give a reason for your answer.

Answer of part (a) is an underestimate because I rounded down the miles per week and the number of miles in a year.



Estimation

1 Work out an estimate for the value of 38.7 x 64.2 11.3

(3 marks)

2 Work out an estimate for the value of 5.4 + 24.05 0.49

(3 marks)

3 Work out an estimate for the value of 19.3 + 52.8 0.12

(3 marks)

4 Work out an estimate for the value of $27.75 + \sqrt{49}$ 0.192

(3 marks)

5 Work out an estimate for the value of $4.93 \times \sqrt{99}$ (2.03)³

(3 marks)

6 Work out an estimate for the value of 6.8 - 2.9

(3 marks)



Estimation

- 7 Sara gets paid £7.21 per hour she works. Each week Sara works 31 hours.
 - (a) Work out an estimate for the amount Sara gets paid in a week.
 - (b) Is your answer to part (a) an underestimate or an overestimate?

Give a reason for your answer.

(3 marks)

8 In a cinema there are 39 rows and in each row there are 23 seats.

Each ticket cost £9.10

Work out an estimate for the total income from the ticket sales.

(3 marks)

- 9 Alice buys 63 apples at 32p each.
 - (a) Work out an estimate for the total cost of apples.
 - (b) Is your answer to part (a) an underestimate or an overestimate?

Give a reason for your answer.

(3 marks)



Estimation

10 Mr. Ronaldo wants to buy a computer for every students in year 12.

There are 197 students in year 12.

Each computer cost £725.

- a) Work out an estimate for the amount of money Mr.Ronaldo spent on computers.
- (b) Is your answer to part (a) an underestimate or an overestimate?

Give a reason for your answer.

(3 marks)

11 James wants to buy some printers and ink cartridges.

Estimate the total cost of 22 printers at £197 each and 78 ink cartridges at £31.10 each.

(3 marks)

12 A roll of wallpaper costs £ 8.95.

Suzi buys 29 rolls of wallpaper Work out an estimate for the total cost of wallpapers.

(3 marks)



Estimation

answers

1 Work out an estimate for the value of 38.7 x 64.2

Solution:
$$38.7 \times 64.2 \approx \frac{40 \times 60}{10}$$

$$= \frac{2400}{10}$$

$$= 240$$

2 Work out an estimate for the value of 5.4 + 24.050.49

Solution:
$$\frac{5.4 + 24.05}{0.49} \approx \frac{5+24}{0.5}$$

$$= \frac{29}{0.5}$$

$$= 58 (29 \times 2)$$

3 Work out an estimate for the value of 19.3 + 52.8 0.12

Solution:
$$19.3 + 52.8 \approx \frac{20 + 50}{0.1}$$

$$= \frac{70}{0.1}$$

$$= 700 \quad (70 \times 10)$$



Estimation

answers

4 Work out an estimate for the value of $27.75+\sqrt{49}$ Solution: 0.192

$$\frac{27.75 + \sqrt{49}}{0.192} \approx \frac{30 + 7}{0.2}$$

$$= \frac{37}{0.2}$$

$$= 185 \quad (37 \times 5)$$

5 Work out an estimate for the value of $\frac{4.93 \times \sqrt{99}}{(2.03)^3}$

$$\frac{4.93 \times \sqrt{99}}{(2.03)^3} \approx \frac{5 \times 10}{(2)^3}$$

$$= \frac{50}{8}$$

$$= 6.25$$

6 Work out an estimate for the value of 6.8 - 2.9 Solution: 0.53

$$\frac{6.8 - 2.9}{0.53} \approx \frac{7 - 3}{0.5}$$

$$= \frac{4}{0.5}$$

$$= 8 \quad (4 \times 2)$$



Estimation

answers

- 7 Sara gets paid £7.21 per hour she works.
 - Each week Sara works 31 hours.
 - (a) Work out an estimate for the amount Sara gets paid in a week.
 - (b) Is your answer to part (a) an underestimate or an overestimate? Give a reason for your answer. **Solution**:
 - (a) $7 \times 30 = £210$ (Sara gets paid in a week)
 - (b) Underestimate because I rounded down the pay and number of hours.
- 8 In a cinema there are 39 rows and in each row there are 23 seats.

Each ticket cost £9.10

Work out an estimate for the total income from the ticket sales.

Solution:

number of rows $\approx 39 = 40$

number of seats $\approx 23 = 20$

one ticket cost = 9.10 ≈ £9

Total seats= 40 x 20 = 800

Total income= 800 x 9 = £7200



Estimation

answers

- 9 Alice buys 63 apples at 32p each.
 - (a) Work out an estimate for the total cost of apples.
 - (b) Is your answer to part (a) an underestimate or an overestimate? Give a reason for your answer. **Solution**:

number of apples = $63 \approx 60$ one apple cost = $32p \approx 30p$

- (a): Total costof apples= 60 x 30 = 180p
- (b): Underestimate because I rounded down both values.
- 10 Mr. Ronaldo wants to buy a computer for every students in year 12. There are 197 students in year 12. Each computer cost £725.
 - a) Work out an estimate for the amount of money Mr.Ronaldo spent on computers.
 - (b) Is your answer to part (a) an underestimate or an overestimate?

Solution: number of students = $197 \approx 200$ one computer cost = £725 \approx £700

- (a): Total money spent=200x700=£140000
- (b): Overestimate because I rounded up the number of students.



Estimation

answers

11 James wants to buy some printers and ink cartridges.

Estimate the total cost of 22 printers at £197 each and 78 ink cartridges at £31.10 each.

Solution:

1 printer cost= £197 ≈ £200 number of printers= 22 ≈ 20

1 ink cartridges cost = £31.10 ≈ £30 number of ink cartridges = 78 ≈ 80

Total cost=(20x200) + (30 x 80) Total cost=4000 + 2400 = £6400

12 A roll of wallpaper costs £ 8.95.

Suzi buys 29 rolls of wallpaper

Work out an estimate for the total cost of wallpapers.

Solution:

one roll cost= £8.95 \approx £9 number of rolls= 29 \approx 30

Total cost=9 x 30 = £270